This paper addresses the issues of unstructured terrain modeling for the purpose of navigation with legged robots. We present an improved elevation grid concept adopted to the specific requirements of a small legged robot with limited perceptual capabilities. We propose an extension of the elevation grid update mechanism by incorporating a formal treatment of the spatial uncertainty. Moreover, this paper presents uncertainty models for a structured light RGB-D sensor and a stereo vision camera used to produce a dense depth map. The model for the uncertainty of the stereo vision camera is based on uncertainty propagation from calibration, through undistortion and rectification algorithms, allowing calculation of the uncertainty of measured 3D point coordinates. The proposed uncertainty models were used for the construction of a terrain elevation map using the Videre Design STOC stereo vision camera and Kinect-like range sensors. We provide experimental verification of the proposed mapping method, and a comparison with another recently published terrain mapping method for walking robots.

Keywords: RGB-D perception, elevation mapping, uncertainty, legged robots.

1. Introduction

To operate autonomously on a previously unknown terrain, a robot has to perceive the environment, build a model, localize itself and plan its motion. Environment perception plays an important role in robot navigation. The robot needs accurate data from sensors to build a model of the environment. This model (map) can be used to adapt the gait to the terrain profile (Walas and Belter, 2011), plan the motion (Zucker et al., 2010) and localize the robot (Yoon et al., 2013), and should thus be designed taking into account the real-time operation of the entire navigation system.

Among many existing representations of the environment (raw point cloud, occupancy map, 2.5D elevation map, triangle mesh, octree (Hornung et al., 2013), multi-level surface (MLS) maps (Pfaff et al., 2007)), we work with 2.5D elevation maps. Motion planning for walking robots is more complex than for wheeled robots. Even if the robot walks statically stable, it needs to select footholds, modify the inclination of the body to actively adapt to the terrain profile, and plan feet and body trajectories. The motion planning procedures have to send many queries about the height of the terrain at a given location. We decided to use a 2.5D elevation map because it provides constant and short access time and most of the planning methods for walking robots are designed to use elevation maps (Belter and Skrzypczyński, 2011a; Belter et al., n.d.; Stelzer et al., 2012). The size of the cell should be similar to that of the robot’s foot to allow for foothold selection. Thus, the resolution of the map for a walking robot should be higher than for a wheeled robot. With increasing computational power, full 3D representations like octree maps (Octomap) become more interesting, but are still more challenging than a 2.5D representation.

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In our system, the map of the environment is updated using data from two types of sensors providing dense depth measurements: a passive stereo camera and an active PrimeSense structured light sensor. The most well-known sensor of this type is Microsoft Kinect, but we use Asus Xtion and PrimeSense Carmine, which are more suitable for legged robots due to their size. As the walking robot should operate in various environments, we are focused on two complementary sensors. The PrimeSense-based sensor returns accurate depth data indoors. Because Kinect and Asus Xtion use near-infrared structured light projectors to obtain information about the distance to the objects, these sensors do not operate outdoors (Belter et al., 2015). Thus, we use a stereo camera, which returns depth data even in direct sunlight conditions. On the other hand, the stereo camera encounters problems whenever the objects in the environment do not contain sufficient visible features. Plain walls and floors, which are very common indoors, are problematic for passive stereo-based perception.

The mapping method presented in this paper is general and can be used with any kind of depth sensor as input to the mapping method. We demonstrate how to use data from two common types of sensors to update the height and uncertainty of each cell of the elevation map.

1.1. Approach and contribution. In this paper we address the problem of perceiving and mapping the environment for walking robots. We present a procedure which updates the height of the cell of the elevation map. To this end, we introduce a new structure of the map. Each cell of our elevation map corresponds to a stack of voxels. This structure allows removal of erroneous measurements which are not filtered by the front-end filtering procedures (that are based on the properties of the depth sensor used for environment perception). We also present an elevation estimation procedure based on a static Kalman filter (KF). The paper also provides methods which better handle occlusions (visibility checking procedure) and erroneous data points introduced by the stereo vision system.

We additionally show how to remove spurious data from stereo images. Most of the artifacts can be found on the edges of objects. The goals of the proposed method are to remove spurious data and to preserve sharp edges. We are looking for a method that is relatively simple and fast in comparison with those known from computer graphics (Dey et al., 2012; Sharf et al., 2007). We show that our technique improves the accuracy of the map in comparison with the embedded filters provided by the Small Vision System (SVS) (Konolige, 1997) software library, and removes less useful 3D points.

We also provide uncertainty models of the sensors used for mapping. We show how the measurement error propagates through the mapping procedure to the uncertainty of each cell of the map. We present an analytical uncertainty propagation procedure for the stereo camera and the PrimeSense-based sensor. This procedure is general enough to be applied to other types of RGB-D and vision sensors, such as time-of-flight (ToF) cameras. Moreover, we provide sensor-specific procedures for filtering the measurement data. We show how to remove incorrect measurements from the point cloud obtained when the stereo camera is used.

The last part of the paper contains an experimental verification of the mapping method. We show the properties of the mapping method, its accuracy and the role of the data filtering procedure proposed in the paper. We also provide experimental results obtained on real walking robots.

This article is a significantly extended version of the conference paper by Łabecki and Belter (2014), which builds also on the previous works of the PUT team (Belter et al., 2012; Łabecki and Skrzypczyński, 2013), and the ETH/ASL team (Fankhauser et al., 2014) concerning perception and mapping for legged robots. In this paper we assume that the environment is quasi-static (it does not change in close vicinity of the robot), and that the robot is well-localized relative to its environment. Therefore, we can focus on efficient estimation of geometric properties of the terrain and the influence of uncertainty in dense depth perception. The initial version of this work was presented at the special session on Robotic perception employing RGB-D images during the 13th National Conference on Robotics in Kudowa Zdrój, Poland, 2014.

2. Related work

Several papers have already addressed the application of stereo vision for terrain mapping. Poppinga et al. (2010) reports the usage of a stereo-on-chip (STOC) camera as a sensor for mobile robots in search and rescue tasks. However, artifacts produced by the camera were not taken into account. Stereo vision has been used for terrain modeling with walking robots so far only in few projects, mostly because typical stereo systems impose high costs of 3D points computation. In the works of Kolter et al. (2009) and Rusu et al. (2009) walking robots with stereo-based perception are shown to autonomously traverse a rugged terrain, but in both cases the computations are performed off-board, and explicit propagation of the spatial uncertainty from the stereo data to the elevation map is not taken into account. The knowledge about the elevation uncertainty of each cell in the map allows planning the path of the walking robot more efficiently, while avoiding uncertain areas (Belter and Skrzypczyński, 2011b). Finally, the uncertainty measure can be used for data fusion in a multi-sensor perception system. In this case each sensor should have its own uncertainty model, but these models have to be expressed in a common framework.
The approach of Kleiner and Dornhege (2007) as well as Fankhauser et al. (2014) is based on the estimation of the motion of the robot. The simplified solution of Kleiner and Dornhege (2007) assumes that the uncertainty of the robot’s position and orientation is reflected in the map by linearly growing the variance of the height estimate based on the accumulated distance and angle. This approach conservatively merges an approximation of the pose uncertainty into the height variance without taking the effect of the in-plane uncertainty into account. The work of Fankhauser et al. (2014) extends this formulation to propagate the full pose uncertainty of the robot to the map. The mapping method presented in this paper does not account directly for the robot pose uncertainty, assuming that a precise pose estimate is available to the robot. This makes computing the elevation values simpler and faster than in the work of Fankhauser et al. (2014). This assumption, when applied to the local area around the legged robot which is in the field of view of the on-board RGB-D or passive camera, is quite realistic, as demonstrated by Belter and Skrzypczyński (2013). For indoor applications, precise pose estimates of a walking robot can be obtained using RGB-D sensing (Nowicki and Skrzypczyński, 2013). On the other hand, the pose uncertainty may be easily added to the updating mechanism, as the underlying data structures are very similar.

Some of the grid-based algorithms for rough terrain mapping use ad hoc formulations for mapping; e.g., Ye and Borenstein (2004) apply heuristics when they fuse consecutive laser range measurements into an elevation grid: their certainty measure is a simple hit/miss counter. On the other hand, there are 2.5D mapping methods which are based on probabilistic foundations. The locus method of Kweon and Kanade (1992) applies a simple geometric approximation in order to obtain the elevation uncertainty from the model of a range sensor’s beam and its interaction with the terrain. However, this method does not propagate explicitly the probabilistic model of range measurements to the uncertainty of elevation. Hebert et al. (1989) build a grid map for a planetary rover in which each cell represents the height of the terrain in order to approximate the surface of the environment. They use matching algorithms to find the corresponding transformation between multiple scans to build a composite elevation map. The authors do not address the issues of error propagation. More recently, a method for efficient volumetric mapping has been presented, which employed the notion of positive and negative occupancy mass to represent the environment (Dryanovski et al., 2010). Although this model is efficient with regard to the map size, it is rather suited for robots that require a full 3D world model, not for walking robots, which can use much simpler 2.5D maps.

An entirely different concept is presented by Plagemann et al. (2008), who propose a non-parametric continuous surface estimation method. This method is based on Gaussian process regression and applies non-stationary covariance functions for adaptation of the regression kernels to the structure of the terrain. It enables filling-in large gaps in elevation data, and provides estimates of uncertainty for the filled-in regions. However, these advantages come at the cost of a high computational burden, which can be prohibitive for a small walking robot.

So far we have not extended our mapping system towards description of multi-level or overhanging objects, such as bridges and tunnels. This can be implemented with multi-level surface maps (Pfaff et al., 2007), but it is not necessary for the legged robot considered, which carries downwards-pointing RGB-D sensors or cameras, mounted in a geometric configuration optimized for terrain surface perception. We use the data from depth sensors directly to create a 2.5D model of the terrain. A similar approach is used on the DLR-Crawler walking robot (Stelzer et al., 2012), which uses data from a stereo camera to model the environment and plan the motion of the robot. They applied the locus method (Kweon and Kanade, 1992), and showed that this method gives denser maps with fewer artifacts than the traditional method for creating a digital terrain model (Stelzer et al., 2012). To minimize the influence of the localization error, existing values on the height map are overwritten by new values.

3. Elevation mapping method

3.1. Mapping method. The aim of the mapping method is to create an accurate model of the environment, which is suitable to be used for motion planning of a walking robot. We chose the elevation map representation of the environment because it allows us to efficiently query the map in the motion planning of the robot on a rough terrain (Belter and Skrzypczyński, 2011a; Belter et al., n.d.; Saarinen et al., 2013). The main problem with this mapping method for a walking robot is related to the perception system and geometrical properties of the obstacles. A mobile robot equipped with on-board
range sensors cannot measure elevation of the terrain directly (Fig. 1). When the robot is close to a high wall or its trunk is tilted down (Fig. 1(b)), it is not possible to estimate the height of the wall by the top part of this obstacle. Assuming that the wall is represented in a 2.5D map, the best estimate of the elevation of the cells related to this wall is the highest measured value in the whole history of measurements for these cells \(h_{[i,j,n_{\text{max}}]}\).

We refer to the (horizontal) cell index in the map with \(i\) and \(j\), and the (vertical) voxel index with \(n\). Note that in the example of Fig. 1 the elevation hypothesis with the lowest variance value \(h_{\text{min}}\) is not a good estimate of the wall height. On the other hand, the maximal height in the history of measurements \(h_{[i,j,n_{\text{max}}]}\) is sensitive to spurious or very sparse measurements. Assuming that the maximal height is estimated solely in a probabilistic framework, like the Kalman filter, a single erroneous measurement might lead to a biased, incorrect estimate of the height of the obstacle (Fig. 1(b)). Our method removes sparse and erroneous measurements before they are fed to the probabilistic estimator, and then uses this estimator to combine the previous estimate of the cell elevation with the most recent measurements, providing an accurate estimate of the cell elevation, \(h_{[i,j]}\).

The simple max height criterion originally proposed by Ye and Borenstein (2004) might cause improper height estimation even if only one measurement exists above the real height of the cell. Thus, we extended this approach, dividing the space above the 2.5D elevation cell into 3D voxels (Fig. 3). This allows us to apply a state estimator, e.g., the Kalman filter, to obtain an optimal estimate of the given voxel’s elevation from noisy measurements. Moreover, we apply a simple column hit counter to reduce the role of sparse and wrong measurements. Then we use another Kalman filter to estimate the elevation of the cell considering the previous estimates of this elevation. This approach separates the process of cell elevation update using measurements taken at various vantage points from the selection of the most appropriate elevation measurement at the given position of the robot. This way our procedure accounts for the qualitative-type uncertainty in the range measurements (Skrzypczyński, 2007) related to the change of the field of view when the robot observes an obstacle from different vantage points.

The diagram of the mapping procedure is presented in Fig. 2. The procedure uses point clouds as input and returns the height of each cell, \(h_{[i,j]}^{(k+1)}\), and the corresponding uncertainty value, \(\sigma_{[i,j]}^{(k+1)}\). Each 3D point is used to update the map. The depth sensor measurements \([x, y, z]^T\) and related uncertainty \(\Sigma_p\) are transformed to the map coordinate system using the estimated position of the robot. The method which allows computing \(\Sigma_p\) from a raw measurement is presented in Sections 4.2 and 4.3. In Section 4.1 we also show how to filter the raw point cloud obtained from the stereo camera to improve the accuracy of the elevation map.

The updated cell is selected according to the \(x, y\) coordinates of the measured point. The distance of the point above the plane, \(h_{m(k+1)}\), as well as the measurement uncertainty, \(\sigma_p^2\), is used to update the elevation estimate of the corresponding voxel in the column above the cell. We use \(n\) separate voxel Kalman filters to estimate the elevation of each voxel. Then, we apply another Kalman filter to estimate the final elevation of each cell (cell Kalman filter). Only the highest estimated value, \(h_{[i,j,n_{\text{max}}]}\), from the voxels updated in the previous step is provided on the input of the cell Kalman filter which is used to estimate the elevation of the cell in the elevation map. Note that the Kalman estimator cannot be applied directly to each cell of the elevation map because the mobile robot cannot directly measure the height of the cell (Fig. 1(b)). A direct measurement is possible if the range sensor measuring the elevation is located high above the ground plane, e.g., on a flying robot. In this case the sensor is much higher than the measured cells, and this configuration allows us to assume that each measurement contains information about the highest object located in each cell.

In the mapping procedure, one-dimensional static Kalman filters are used to estimate the height of the voxels. Another Kalman filter is used to estimate the height of each cell. To transform the uncertainty from the camera frame to the map coordinate system, we use the procedure described in Section 4.2. The variances of the
height measurements $\sigma^2_{z_{(k+1)}}$ are used as weights in the voxel’s Kalman filters. All measurements inside the voxel considered are used to update the hypothesis about the height of that voxel. The state vector and measurement are the height of the voxel and measured height, respectively. The state transition and projection models are identity mappings. We initialize the state of the filter with the initial height of the cell (the state of the filter) is zero.

For all updated voxels in the column considered we choose the cell with the highest elevation value, $h_{(k+1)}^{[i,j,n]}$. This cell has the vertical index $n_{\text{max}}$, and a corresponding variance $\sigma^2_{h_{(k+1)}^{[i,j,n]}}$. The parameters of the selected voxel, $h_{(k+1)}^{[i,j]} = h_{(k+1)}^{[i,j,n_{\text{max}}]}$ and $\sigma^2_{h_{(k+1)}^{[i,j]}} = \sigma^2_{h_{(k+1)}^{[i,j,n_{\text{max}}]}}$, are used to compute the elevation and the uncertainty of the whole column (the cell of the elevation map). The state vector and measurements of the Kalman filter in each cell are the height of the cell, $h_{(k+1)}^{[i,j]}$, and measured height, $h_{(k+1)}^{[i,j]}$, respectively. As in the voxel filter, the state transition model and projection model are identity mappings. The initial height of the cell (the state of the filter) is zero.

The elevation, $h_{(k+1)}^{[i,j]}$, and the uncertainty, $\sigma^2_{h_{(k+1)}^{[i,j]}}$, are computed as follows:

$$K_k = \sigma^2_{h_{(k)}^{[i,j]}} \left( \sigma^2_{h_{(k)}^{[i,j]}} + \sigma^2_{z_{(k+1)}} \right)^{-1},$$

$$h_{(k+1)}^{[i,j]} = h_{(k)}^{[i,j]} - K_k \left( h_{(k)}^{[i,j]} - h_{(k+1)}^{[i,j]} \right),$$

$$\sigma^2_{h_{(k+1)}^{[i,j]}} = (1 - K_k) \sigma^2_{h_{(k)}^{[i,j]}}.$$

In (2), $K_k$ is the Kalman gain computed for the column $[i,j]$, $\sigma^2_{h_{(k)}^{[i,j]}}$ is the value of the variance for the column $[i,j]$ at time $k$, and $h_{(k)}^{[i,j]}$ is the elevation value for the column $[i,j]$ at time $k$. The new elevation of the column at time $k+1$ and the new variance at time $k+1$ are $h_{(k+1)}^{[i,j]}$ and $\sigma^2_{h_{(k+1)}^{[i,j]}}$, respectively.

The procedure of voxel and grid cell update is presented in Fig. 3. Each voxel is updated using new measurements (Fig. 3(b)). The measurements are aggregated for each voxel using (1), as shown in Fig. 3(c).

Fix Fig. 3. Concept of the map update procedure: the map is divided into voxels (a), new measurements on the global map (b), the new measurements are aggregated for each voxel using Kalman filter (c), the highest value in the column is used to update the elevation map (d), (e).

Then, the highest value from the updated voxels for the whole column is selected (Fig. 3(d)), and used to compute the new height value in the global elevation map and the uncertainty value (Fig. 3(e)). Note that the map updating procedure might lead to height reduction of the cell (Fig. 3(e)).

We reduce the importance of isolated and old measurements using a measurements vitality counter (cf. Fig. 2). To consider the column a correct one, a minimal number of measurements in the specified time has to be collected. Whenever the sensor provides measurements of the values inside the column, the counter $V$ for the column considered is increased by the value $V_d$. If the whole column is not updated during the map updating procedure, the counter is decreased by the value $V_i$. The starting and minimal value for each counter $V$ is 0. If the counter value is bigger than a threshold $V_t$, then the counter is locked, the mapping procedure considers the column established, and the measurements are used to update the map. During the experiment we use $V_i = 3$, $V_d = 2$, $V_t = 7$. An example counter state during the map
3.2. Post-processing. To reduce the influence of artifacts introduced by the sensor noise, we check the visibility of each updated cell. The visibility checking procedure is performed after all the individual cells have been updated. The order of cell visitation is from the most distant to the nearest one. We assume that the cell which is updated has to be visible from the current pose of the sensor. Thus, if an existing cell \( c_{i,j} \) occludes the updated cell, we assume that the existing cell contains erroneous measurements. To check the visibility constraint, we increase the height of the cells by their uncertainty, i.e., \( h_{i,j} + 3\sigma_{i,j} \). Thus, the probability that the real height of the cell is below this threshold is 0.99. Moreover, the updated cell should be matured—the vitality counter value should be stabilized. If the vitality value of the updated cell is above the threshold, we remove the voxels from the occluding cell \( c_{k,l} \) which are above the line of sight. This concept is presented in Fig. 5.

The result of the procedure on a real elevation map is presented in Fig. 6. Note that the update of a single cell might remove many existing and occluding cells. In practice, the criteria are very strict and most of the occluding obstacles are removed. We found this useful when the localization system was not precise enough. In the case of strong slippage which is not compensated by the localization system, the most recent measurements are the most accurate and they overwrite the old measurement.

Finally, median filtering is performed using a 2D sliding window on the elevation map. It allows removing small artifacts and fill-in small missing areas of the elevation grid.

4. Terrain perception

The mapping method requires a point cloud as an input. In our research we use two type of sensors: a stereo camera and a PrimeSense-based device (Kinect, Carmine, Asus Xtion). These sensors have various properties, and thus we defined two separate filtering methods and uncertainty models.

4.1. Perception using a stereo camera. For outdoor experiments we prefer to work with the stereo camera. The passive camera provides data in various light conditions. We use the Small Vision System (SVS) software proposed by Konolige (1997). The library provides an implementation of the correlation-based stereo algorithm and returns a point cloud which corresponds to the configuration of the detected object. The SVS uses visual features to match pixels from the left and right images. Whenever the camera observes smooth surfaces without visual features, the SVS library does not return information about the distance to the obstacle. Even worse, if the camera observes objects with repeated patterns (texture), the returned data are erroneous. Fortunately, these types of objects are more common indoors. In outdoor natural environments, the obstacles are feature-rich and repeated patterns are typically rare. However, the data obtained from the passive stereo camera have do be filtered in order to remove artifacts.
Because the filters embedded in the SVS do not remove all artifacts, we propose new methods which process the data obtained from the stereo camera. The artifacts which cannot be removed by the embedded filters occur whenever that of the object differs significantly from the disparity of the background (edges of the objects). As a result, halos which span the space between the edge and the background can be visible in the resulting point cloud (Fig. 7(d)). The second group of erroneous measurements consists of points on reflective surfaces and out-of-horopter artifacts. Such artifacts create a group of points close to the current camera pose (Fig. 7(c)). We remove all of the mentioned erroneous measurements by analysis of the depth image (Fig. 7(b)). The image can be obtained by projecting the point cloud on the image surface, or directly, using the available disparity image values:

$$z = \frac{bf}{d},$$  \hspace{1cm} (3)

where $z$ is the depth value, $b$ is the baseline of the stereo camera (the distance between coordinate systems of the left and right image), $f$ is the focal length, and $d$ is the disparity value.

The value of a pixel which does not have corresponding measurements (e.g., when the SVS did not find a correct correspondence between stereo images or the measurements are removed by the embedded filters) is 0, which is represented as a black background in the images.

To remove erroneous measurements, the empty regions in the images are filled in using the mean values of each row and column on the image (Fig. 8(b)). For each pixel $[u, v]^T$ the mean value is computed as follows:

$$a = \frac{\sum_{i=1}^{h} d(u, i) + \sum_{j=1}^{w} d(j, v)}{N_u + N_v},$$  \hspace{1cm} (4)

where $w$ and $h$ are the width and height of the image, respectively, $N_u$ and $N_v$ are the number of non-zero pixels in row $u$ and column $v$ of the depth image, $d(u, i)$ and $d(j, v)$ are the intensity values of the depth image.

After filling in the empty regions, the image is smoothed using a median filter. The window size of the filter is chosen to be 75 pixels. Image smoothing removes
pixels which differ significantly from the background, which are typically erroneous pixels resulting from measurement artifacts (Fig. 8(c)). Then, the smoothed image is subtracted from the original image (Fig. 8(d)). We create a mask using the output image. The pixels which differ by less than 10% from the smoothed image are used to form the mask (Fig. 8(e)). The mask is used to remove artifacts. Occasionally, empty spaces in the image may arise for small groups of pixels, and they are removed by morphological openings (erosion and dilation) on the mask image (Fig. 8(f)) (Szeliski, 2011). When the mask is applied, most of the artifacts are removed from the original image. The point cloud before and after the artifact removing procedure is shown in Fig. 9.

4.2. Uncertainty model of stereo measurements. The mapping procedure requires not only 3D measurements in the input but also their uncertainty $\Sigma_p$ (Fig. 2). Because the information about the uncertainty of measurements is not returned by sensors used in this research, we present methods which allow us to determine $\Sigma_p$ for two most popular depth sensors.

Analysis of the sensory data used for map building is difficult without knowledge of the underlying uncertainty of the measurements (Thrun et al., 2005). In the mapping scenario with a stereo camera as a sensor, the computation of uncertainty should be fast. The application of the robot in real environment missions requires real time operation of the mapping method. The uncertainty model should determine the influence of the camera resolution and calibration errors on the uncertainty of the coordinates of each point in the point cloud and finally the uncertainty of the cell of the elevation map. Matthis and Shafer (1987) proposed to use 3-dimensional Gaussian distributions to represent the measurement error of raster-based sensors (e.g., a visual camera). It was shown that the uncertainty model represented by the covariance matrix of 3D coordinates reduces the localization error in SLAM (Skrzypczyński, 2009). Sahabi and Basu (1996) presented a method to compute the optimal configuration of the stereo camera, which decreases the error of the depth measurement. The optimization is possible because the uncertainty model of the camera is available.

In stereo triangulation methods, the main sources of measurement errors are related to the finite resolution of the image and wrong correspondences between the images. Because both correspondence and depth are determined on the basis of rectified images (while the rectification procedure uses the calibration parameters), the uncertainty of the calibration also influences that of the measurement. It is very difficult to analyze wrong correspondences due to their random nature, so this source of measurement errors was ignored. The remaining factors are analyzed using analytical methods (Łabecki and Skrzypczyński, 2013).

The procedure of uncertainty computation is presented in Fig. 10. First, we determine the relation between the position of the pixel in the image without distortion $[x_u, y_u]^T$ and the position of the pixel in the distorted image $[x_d, y_d]^T$:

$$[x_u, y_u]^T = f([x_d, y_d]^T).$$

The formula (5) is determined by the linearization of the distortion equations and depends on the distortion parameters $k_1$, $k_2$, $k_3$, $p_1$, $p_2$ and intrinsic camera parameters $f_x$, $f_y$, $c_x$, $c_y$ found during the calibration procedure. Propagating the uncertainty, we can compute a covariance matrix on the image without distortion:

$$\Sigma_u = J_u \Sigma_d L J_u^T,$$  

Fig. 9. Point cloud before (artifacts are indicated by the arrows) (a) and after the artifacts removal procedure (b).
where $J_u$ is the Jacobian of (5) with partial derivatives with respect to $(k_1, k_2, k_3, p_1, p_2, f_x, f_y, c_x, c_y)$. $\Sigma_{dl}$ is the covariance matrix of distortion and intrinsic camera parameters.

Similarly, the uncertainty propagates through the rectification algorithm:

$$\Sigma_{rL} = J_{rL} \Sigma_{ueL} J_{rL}^T, \quad (7)$$

where $J_{rL}$ is the Jacobian of the rectification equation with respect to pixel coordinates in the image without distortion and extrinsic parameters of the camera $(x_u, y_u, T_x, T_y, T_z, \theta_x, \theta_y, \theta_z)$, $\Sigma_{ueL}$ is the covariance matrix of the pixel’s coordinates on the image without distortion and extrinsic parameters of the camera, $\Sigma_{rL}$ is the covariance matrix of the pixel’s coordinate on the rectified image.

Taking into account the uncertainty of the position of a pixel in the rectified images, the uncertainty of the disparity can be defined as follows:

$$\sigma_d = \sigma_{u,r} + \sigma_{w,r}, \quad (8)$$

where $\sigma_{u,r}$ and $\sigma_{w,r}$ are standard deviations in the row $u$ of the left and right image, respectively.

The covariance matrix of the 3D point $p = [x_v, y_v, z_v]^T$ is computed as follows:

$$\Sigma_p = J_p \Sigma_{rp} J_p^T, \quad (9)$$

where $J_p$ is the Jacobian of $p$ with respect to $d$, $u_r$, $v_r$, and extrinsic parameters of the stereo camera, $\Sigma_{rp}$ is the covariance matrix of the disparity $d$, the position of the pixel on the rectified image $[u_r, v_r]^T$, and extrinsic parameters of the stereo camera.

### 4.3. Uncertainty model of PrimeSense measurements.

In our research, we also use PrimeSense-based sensors (Kinect and Asus Xtion). We employ these without any additional filtering procedures. The point cloud is used as the input of the mapping algorithm.

As with the stereo camera (Section 4.2), we apply a similar mathematical procedure to describe the uncertainty model of the PrimeSense sensor. The uncertainty model is based on the solution proposed by Park et al. (2012). First, the relation between the position of a pixel in the depth image and the 3D position of the point is defined:

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \frac{1}{f_x} & 0 & -\frac{C_x}{f_x} \\ 0 & \frac{1}{f_y} & -\frac{C_y}{f_y} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ 1 \end{bmatrix}, \quad (10)$$

where $u$ and $v$ represent the position of the pixel in the depth image and $d$ is the depth measurement value. Variables $f_x$ and $f_y$ are the focal length parameters and $C_x$ and $C_y$ are optical axis parameters of the depth camera.

To transform the uncertainty from the camera frame to the map coordinate system, we use the procedure described in Section 4.2. Then, we can compute uncertainty of each point in the cloud:

$$\Sigma_p = J_p \Sigma_{u,v,d} J_p^T, \quad (11)$$

where $J_p$ is the Jacobian of (10) with respect to $u$, $v$, and $d$, while $\Sigma_{u,v,d}$ is the covariance matrix of image coordinates $u$, $v$ and depth $d$. The values of the variances $u$ and $v$ are constant but the variance $\sigma_d$ of depth $d$ depends on the current depth measurement. We approximate the relation found experimentally by Khoshelham and Elberink (2012) using

$$\sigma_d = k_1 d^3 + k_2 d^2 + k_3 d + k_4, \quad (12)$$

where $k_1, \ldots, k_4$ are constants. The obtained uncertainty model is presented in Fig. 11.

### 5. Results

#### 5.1. Accuracy of the mapping procedure.

The presented mapping method was used to build a map indoors in the laboratory as well as in an outdoor environment. The obstacles perceived by the system are typical for rough and unstructured environments.

A map of the rough terrain mockup created in the laboratory is shown in Fig. 12.

The stereo camera is mounted 0.8 m above the ground on a cart which can move forward. The sensor is tilted down by 35°. Measurements are performed with a step of 0.1 m. We verified the method which removes artifacts from the stereo measurements. It is difficult to qualitatively assess the number of removed artifacts or wrong measurements. Thus, we compare the overall gain by computation of the difference between the map obtained in the experiment considered and the ground truth map. The influence of the method on the quality...
of the map is measured using a modified version of the performance index (PI) (Ye and Borenstein, 2004):

$$PI = \frac{\sum_{i=1}^{n} \sum_{j=1}^{m} o_f(i, j) (h_f(i, j) - h_t(i, j))^2}{\sum_{i=1}^{n} \sum_{j=1}^{m} o_m(i, j) (h_m(i, j) - h_t(i, j))^2 N_{om}}$$

where $h_f(i, j)$ is the height of the cell $i, j$ of the map which is built using filtered data from the stereo camera, $h_m(i, j)$ is the height of the cell $i, j$ of the map which is built using raw data from the stereo camera, $h_t(i, j)$ is the height of the cell $i, j$ of the ground truth map. The coefficients $o_f(i, j)$ and $o_m(i, j)$ are set to 1 if the height of $h_f(i, j)$ and $h_m(i, j)$ is measured by the sensor and to 0 if no data are available for that cell. $N_{om}$ and $N_{of}$ are the numbers of measured cells in raw and filtered maps, respectively. The PI value is the quotient of the mean squared error (MSE) of the two mapping methods. To obtain the ground truth map, the Hokuyo laser scanner was attached to an industrial robot arm and moved horizontally above the mockup (in $x$ and $y$ directions).

The resulting maps of the terrain mockup obtained by different variants of the elevation mapping method are presented in Fig. 13. The PI value for the map which is built from the stereo data obtained from the mapping method which uses the proposed data filtering procedures is 0.91. The MSE is reduced by 9%. The PI is 0.99 for the map obtained from stereo data filtered by the embedded SVS filters with default settings. This map contains empty regions which are not visible in the map, built using the most tolerant settings of the embedded filters. This means that the embedded filters improve the mapping quality by 1% in comparison with the map built from a raw point cloud, but they remove useful data.

We also compared the use of a stereo camera (STOC) with an Asus Xtion sensor in the mapping procedure. The PI value computed for the map using Asus Xtion (Fig. 13(d)) and the stereo camera with the proposed data filtering method (Fig. 13(c)) is 0.59. This means that the MSE is reduced by 41% when Asus Xtion is used, from which we conclude that it provides much more accurate data than the stereo camera. Moreover, Asus Xtion provides depth data of regions which are plain and textureless. The floor is easily visible on the map created from the Asus Xtion data (Fig. 12(c)). The only invisible regions are caused by occlusions. On the map from the stereo camera (Fig. 12(b)) only the mockup is visible.

5.2. Influence of the localization error. A map obtained from experiments with the stereo camera mounted on a robotic manipulator is presented in Fig. 14. The robotic arm provides accurate localization of the sensor, thus we only investigate the properties of the mapping method. The maps presented in Fig. 14(a)–(f)
are obtained from the consecutive snapshots. The distance between scans is 0.1 m. Each map in Fig. 14 (a)–(f) is created using individual snapshots. The final map created by the mapping method proposed in this paper is presented in Fig. 14(h). The empty regions which are visible in Fig. 14 (a)–(f) are filled in in the final map. The main problems are connected to deeper concavities on the mockup, which are occluded by higher obstacles. The camera does not provide data about these regions, or data are incorrect due to artifacts which are not removed by the filters.

To check the influence of the localization error on the mapping method, we computed the performance index for two maps created using the proposed filtering and mapping methods. The first map is created on the robotic arm, which provides precise localization of the camera (Fig. 14(h)), and the second is created using the rail (Fig. 13(c)). The computed PI value is 0.86, which means that with the more precise localization system, we were able to reduce the mapping error by 14%. This shows that the proposed mapping method requires precise localization to work properly. For this purpose, parallel tracking and mapping method (Belter and Skrzypczyński, 2013) or RGB-D SLAM (Belter et al., 2015) can be used. Our experience shows that the localization error of these methods is below 2 cm for small workspaces with a sufficient number of visual features.

The results which show the quantitative improvement of the obtained map are summarized in Table 1.

<table>
<thead>
<tr>
<th>Method 1</th>
<th>Method 2</th>
<th>Error reduction</th>
</tr>
</thead>
<tbody>
<tr>
<td>Artifacts removal</td>
<td>Raw SVS data</td>
<td>9%</td>
</tr>
<tr>
<td>Asus Xtion</td>
<td>Stereo camera</td>
<td>41%</td>
</tr>
<tr>
<td>Improved localization</td>
<td>Sensor on a rail</td>
<td>14%</td>
</tr>
</tbody>
</table>

5.3. Experiments on a real robot. In the first experiment on a real robot, we conducted trials with the six-legged Messor robot (Belter and Walas, 2014) with an on-board stereo camera. The robot updates the map at the end of each 10 cm step. During the experiment the robot made 10 steps. The experimental setup and the obtained map are presented in Fig. 15. The map contains only partial information on the environment due to the limited...
camera viewing angle. While the robot has information about obstacles which are in front of it, obstacles which are sideways are not visible on the map. In this experiment we do not have a ground truth elevation map, and thus it is not possible to compute the mapping accuracy. However, the map contains a representation of the obstacles from the real environment (marked by the arrows in Fig. 15(b)).

In the second experiment we created an unstructured environment of ca. 4×3 m and traversed it with the quadrupedal robot StarlETH (Hutter et al., 2012) (Fig. 16(a)). The robot is commanded to walk from one end to the other, turn around, and walk back to the starting point (Fig. 16(c)).

The terrain is measured and mapped continuously as the robot walks with a PrimeSense Carmine 1.09 (short range) structured light sensor which is attached at the front of the robot. Localization is limited to on-board proprioceptive sensing, and consists of the fusion of legged kinematics and inertial measurements (Bloesch et al., 2013). This state estimation is prone to drift in position and yaw orientation. Comparison with motion capture data shows that the on-board state estimator accumulated a position error of 0.3 m and a yaw angle error of 20° for the base of the robot after the entire run. For evaluation, we recorded ground truth measurements with the Leica Nova MS50 MultiStation laser scanner (Fig. 16(b)). The terrain was scanned from three different perspectives and aligned with the built-in tools of the device.

The mapping error in this experiment is mainly caused by the localization method. The resulting maps differ significantly because of the drift of the localization method. This can be observed, for example, with the board on the ground truth map indicated by the arrow number 4 in Fig. 17(a) being shifted by about 1 m on the obtained maps (Fig. 17(b) and (c)). For the maps obtained from this experiment, we computed the performance index to compare the one presented in this paper with the method proposed by Fankhauser et al. (2014). The obtained value is 1.0308, which means that the MSE is bigger by 3% when our method is used. The obtained maps are similar and the difference in the PI value is insignificant.

5.4. Comparison. We compare our method with the one proposed by Fankhauser et al. (2014) because it is the most similar state of the art mapping method with respect to application. There is no fair quantitative comparison with very precise methods known from computer graphics, which are computationally expensive (Berger et al., 2014; Dey et al., 2012) or require user input for surface reconstruction (Sharf et al., 2007). They cannot be applied as a mapping method for a real robot, which has limited computational resources.

Since the quantitative comparison between the presented mapping method and the one proposed by Fankhauser et al. (2014) does not provide clear conclusions, we provide a qualitative comparison and discussion. The first difference between these two methods is indicated by the arrow 1 in Fig. 17(b) and (c). The mapping method presented in the paper is supported by the technique which fills in empty areas in the map. In this case, we use a median filter, which is fast and efficient. To fill in larger areas, more advanced methods based on Gaussian regression can be used (Belter et al., 2012). The map created by the mapping method presented in this paper contains 13730 updated cells, while the compared mapping technique contains 13403 cells. The method which fills in empty areas can nicely reconstruct the parts which are not visible to the robot due to occlusions.

The proposed updating procedure, which is based on the Kalman filter and the column of voxels, results in more realistic shapes of the obstacles on the obtained map. The obstacles indicated by the arrow 2 in Fig. 17(c) have sharp edges which are close to the shape of the real objects (cf. Fig. 16(c)). The obstacles in Fig. 17(b) have filled edges.

The last properties are related to the precision of robot localization. The mapping method proposed by Fankhauser et al. (2014) takes into account the uncertainty of the robot’s pose. This results in generally smoother maps, as indicated with the area 5 in Fig. 17(b) and (c). Another property is that new data play a more important role when the map is updated. Due to the localization

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1For this comparison we only take into account the measurement and model update steps and neglect the map fusion process of the algorithm introduced by Fankhauser et al. (2014).
error, the cells which were updated recently are treated as more accurate than old cells on the global map. This is advantageous as obstacles might shift in the map from the robot’s perspective, and the previously gathered information needs to be updated to reflect the newly acquired data. In this experiment, parts of the terrain are observed twice: first when the robot walks in one direction, and the second time when the robot returns to its original position. As an example, the obstacle indicated by the arrow 3 on the map in Fig. 17(b) is observed at this location only as the robot passes it a second time. While the method by Fankhauser et al. (2014) reflects these changes, our technique (Fig. 17(c)) does not capture this obstacle. This limitation is caused by the assumption that the environment is static and the localization error is small. On the other hand, this behavior is advantageous when the localization error is significant. In this case the local map used for motion planning (Belter and Skrzypczyński, 2011a) is more accurate, despite the fact that some obstacles vanish from the global map.

Table 2. Results of quantitative comparison.

<table>
<thead>
<tr>
<th>Method</th>
<th>Our approach</th>
<th>NDT-OM</th>
<th>Octomap</th>
</tr>
</thead>
<tbody>
<tr>
<td>MSE [m²]</td>
<td>0.063</td>
<td>0.127</td>
<td>0.524</td>
</tr>
</tbody>
</table>

We also compared the mapping method presented in the paper to NDT-OM (Saarinen et al., 2013) and Octomap (Hornung et al., 2013). We verified all three methods on the ICL-NUIM ‘living room’ dataset (Handa et al., 2014). The dataset contains a synthetic sequence of depth and RGB images, with and without noise. It allows the creation of a perfect ground truth map for comparison. The noisy dataset is used for testing. Because our method is designed to estimate the surface of the terrain and cannot handle multi-level maps, we removed points which represent the ceiling in the dataset. Because each compared method has its own environment representation, the environment models from Octomap and NDT-OM are transformed to the elevation map and then compared with the ground truth map. We compare the elevation map obtained from a noisy dataset with the ground truth map created for the same method using a noise-free dataset.

For each method we compute the mean squared error between the ground truth map and the map obtained for noisy data. With the default configuration of mapping systems, the MSE for our method is 0.074 m², while for NDT-OM and Octomap the error is bigger than 1 m². NDT-OM and Octomap are designed to be general and store all 3D noisy measurements in the map structure. When the 3D representation is transformed to 2.5D, the voxels which contain noisy data disturb the structure of the 2.5D maps. Thus, we remove all uncertain voxels from the maps. As a threshold we use $\sigma_h^{(i,j)}$ in our method and the occupancy value for NDT-OM and Octomap. The obtained results are presented in Table 2. Our method still performs the best of all compared methods. The MSE for our mapping method is 50% smaller than the error for NDT-OM. Also, the obtained map presented in Fig. 18(b) contains the least number of artifacts introduced by noisy data. Note that in these experiments we do not
use the artifact removal procedure presented in this paper. We compare mapping methods only and the same noisy sequence of point clouds is provided to the input of each of the mapping methods.

6. Conclusions

This article presents a mapping method for walking robots based on 3D depth sensors. The main contributions of this work are as follows:

- a real-time mapping method with a unique updating procedure which uses the Kalman filter for cell height estimation and a stack of voxels to accumulate measurements;
- a set of procedures which remove erroneous measurements and cells from the map (the vitality counter and the visibility checking procedure);
- a data filtering procedure which improves the quality of point clouds obtained from the stereo camera;
- an uncertainty model for the stereo camera and PrimeSense-based measurements; we show how the uncertainty of the measurement propagates to the uncertainty of the cell height;
- extended experimental verification of mapping, which demonstrates the importance of the particular properties of the mapping method with respect to the elevation map quality, as well as the role of the selected sub-procedures.

In this article we also provide the results of the experiments on two different walking robots. We compare the presented method with that recently proposed by Fankhauser et al. (2014) and discuss the differences between these two methods. We point out the advantages of the method on the maps obtained in the experiment with the real robot and also show its limitations.

In the future we are going to take into account the uncertainty of the robot’s pose in the updating procedure to reduce the influence of localization drift on the map quality. This will be helpful in assessing the quality of data in situations where the robot has not observed a region and has moved away from/over it. We are also going to integrate our mapping method with the terrain classification algorithm (Walas and Nowicki, 2014) to create an object-aware navigation system for legged robots.

Note. The data set with the robot StarlETH used in Section 5.3 is publicly available under the section Terrain Mapping at projects.asl.ethz.ch/datasets.

Acknowledgment

This research was financed in part by a Polish National Science Centre grant funded according to the decision DEC-2013/09/B/ST7/01583. This work was partially supported by the Swiss National Science Foundation (SNF) through the project 200021_149427/1 and the National Centre of Competence in Research Robotics.

References


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Received: 3 October 2014
Revised: 29 April 2015
Re-revised: 4 October 2015